ANALYSIS OF DIFFERENT LOADS AFFECTING THE URBAN RAILWAY TUNNEL SYSTEMS OF CAIRO METRO UNDERNEATH THE RIVER NILE

Hamdy.H.A.Abd-el.rahim¹, Mahmoud Enieb², Ahmed Abdelmoamen Khalil³,
Abdou SH.Ahmed⁴
¹, ², ⁴ Department of Civil Engineering, Assiut University, Assiut, 71516, Egypt
³ Department of Civil Engineering, Shoubra faculty of Engineering, Benha University Benha, 11629, Egypt

Received 11 May 2014; accepted 1 October 2014

Abstract: The study objective of this paper is analysis of different loads affecting the urban railway tunnel systems to determine the optimum tunnel system (single tunnel or twin tunnel). A case study is The Greater Cairo metro line No. 4, which passes under the River Nile in Egypt land. Analysis of settlement and stresses was carried out using three different finite element programs (Ansys, Plaxis and Rocscience Phase). We obtained optimum dimension of the model for the different tunnel systems. Also, vertical and horizontal bed River Nile settlements were computed for single and twin tunnel by the above mentioned programs. The comparison between the two systems in terms of bending moments and settlement is presented. Also, the procedures of construction of the twin tunnel underneath the River Nile were discussed. Moreover, the effect of the train loads on the settlement profile and the horizontal displacement of bed River Nile were evaluated for single and twin tunnel systems. Based on the calculated result, higher stresses in bottom tunnel (twin tunnel system) increased by 100% about stresses in a single tunnel. When trains pass through the tunnel, stresses decrease about 10% for single tunnel and about 5% for twin tunnels.

Keywords: railway, tunnel systems, stresses, finite element analysis, deformations.

1. Introduction

The River Nile which runs through Cairo gives it an attractive and gorgeous view. The urban center is crowded with people, so tunnels and bridges have been constructed to transport large numbers of people across the river. Bridges cause traffic congestion along the roads going to the bridge. Therefore, the optimal solution for the conveyance of the people is tunnels. Especially if the tunnels were extended and connected as subway network under the city.

The Great Cairo Region is a premier city in Egypt. It is rich in history and boasts of a large number of historic structures. It is a large city in the Africa and the Middle East Region. Phase No.1 of line No. 4 will extend from El-Malek El-Saleh station on line No. 1 to Remaya square station as shown in Fig. 1. It will meet the route of line No. 2 in Giza station. The study area for Greater Cairo Metro Line No. 4 starts from Station No. 1 (El-Malek El-Saleh) and extend up to Station No. 5 (El Mesaha Station).

²Corresponding author: ahmed.khalil@feng.bu.edu.eg
Moller (2006) studied the internal forces in tunnel lining and displacement of soil and found that tunnel design needs an honest idea of surface settlements and lining internal forces. Garner and Coffman (2012) found that the design of the tunnel depends on the induced settlement in the tunnel. Therefore, they proposed method giving acceptable ground surface settlement profile to generate a tunnel system configuration, as well as the proposed characterization method can be used to help designers to eliminate potential configurations that would cause excessive surface settlements. Chen et al. (2012) concluded that a good estimation of surface settlement is very important to the construction of tunnels in very crowded cities because failure of neighboring structures due to extra surface settlement above the tunnels, they examined the interaction of multi-tube tunnels on ground surface settlement and the methods of prediction for the transverse ground surface settlement profile. Wang et al. (2012) found that for shallow tunnels constructed in clay soil, a surface settlement above tunnels depend on the creep of soil, they concluded that behaviour of clay creep is very important for long term settlement above the tunnel. Mazek and Almannaie (2013) used finite element analysis to determine the model dimension of cross section for line No. 3 at Cairo metro and he found that minimum width equal to ten times of the diameter of the tunnel. Migliazza et al. (2009) computed vertical settlement of ground surface during excavation and using empirical method and finite element analysis, they found numerical data similar to experimental data. Wang and Su (2011) compared the ground settlement by using the Ansys program and by using excavation program data, they found that it is possible to use Ansys program compared with the original data in excavation program. Mazek (2011) forecasting performance of EL-Azhar tunnel systems, he used finite element model to analyse twin tunnel construction, and concluded that the computed surface settlement different from measurement data in the field by 10%. Chehade and Shahrou (2008) concluded that construction of tunnels causes movement of soil and staining action in lining of the tunnel, also the procedure of construction impact on soil settlement and lining forces.
2. Train Axle Load

Axle load of trains of Cairo metro line No. 4 equals to 16 tons as shown in Fig. 2 (Khalil, 2002; Nejati et al., 2012).

![Train Axle Load for Cairo Line No. 4](image)

3. Geological Profile

Fig. 3 shows the geological section based on the obtained data from the National Authority of Tunnels (NAT) in Cairo. In this figure, there are three main soil layers namely, very dense sand, Silty-sand and Silty-Clay. The physical and mechanical properties of these layers are documented in Table 1 and Table 2. Most of the tunnel is planned to run through the very dense sand layer. The physical and mechanical properties of concrete segment were documented in Table 3. Site investigations along line No. 4 alignment indicate that the soil profile cross section under River Nile as shown in Fig. 4.

![Generalized Geological Profile with Station and Rail Levels](image)

*Source: JICA Project document (2011)*
Table 1
Soil Parameters Sand Layers

<table>
<thead>
<tr>
<th>Soil layers Parameters</th>
<th>Dense Sand</th>
<th>Very Dense Sand</th>
<th>Silty-Sand</th>
</tr>
</thead>
<tbody>
<tr>
<td>Saturated unit weight, $\gamma_{sat}$ (KN/m$^3$)</td>
<td>19.00</td>
<td>20.00</td>
<td>20.00</td>
</tr>
<tr>
<td>Angle of internal friction $\Phi$</td>
<td>36°</td>
<td>38°</td>
<td>38°</td>
</tr>
<tr>
<td>Young’s modulus, $E$ (MPa)</td>
<td>75</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Poisson ratio ($\mu$)</td>
<td>0.29</td>
<td>0.28</td>
<td>0.28</td>
</tr>
</tbody>
</table>

Source: JICA Preparatory study (2012)

Table 2
Soil Parameters for Clay Layer

<table>
<thead>
<tr>
<th>Soil layers Parameters</th>
<th>Silty-Clay</th>
</tr>
</thead>
<tbody>
<tr>
<td>Saturated unit weight, $\gamma_{sat}$ (KN/m$^3$)</td>
<td>19.0</td>
</tr>
<tr>
<td>Undrained shear strength $C_u$ (KN/m$^2$)</td>
<td>20.0</td>
</tr>
<tr>
<td>Undrained Young’s modulus, $E$ (MPa)</td>
<td>30.0</td>
</tr>
<tr>
<td>Drained shear strength $C$ (KN/m$^2$)</td>
<td>2.00</td>
</tr>
<tr>
<td>Angle of internal friction $\Phi$</td>
<td>20°</td>
</tr>
<tr>
<td>Poisson’s ratio ($\mu$)</td>
<td>0.40</td>
</tr>
</tbody>
</table>

Source: JICA Preparatory study (2012)

Table 3
Material Properties of Concrete Segment

<table>
<thead>
<tr>
<th>Material Properties</th>
<th>Concrete</th>
<th>Reinforcement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Design Standard Strength (MPa)</td>
<td>$f_{cu} = 50$</td>
<td>$f_y = 360$</td>
</tr>
<tr>
<td>Modulus of elasticity, $E_c$ (MPa)</td>
<td>31500</td>
<td>$2*105$</td>
</tr>
</tbody>
</table>

Source: JICA Preparatory study (2012)

Fig. 4.
Geological Cross Section Profile of Cairo Metro Line 4 in the Study Area
Source: Ardaman-ACE (2009)
4. Problem Statement

The tunneling section of line No. 4 (phase No. 1) will be constructed by Tunneling Boring Machines (TBM). The arrangement of TBMs and positions of starting diggings are illustrated in Fig. 5. The contractor proposed a tunneling system that is twin tunnels with single track. In this study, the analysis of this system with another system proposed by the authors which is a single tunnel with two tracks, as shown in Fig. 6, will be presented. The proposed cross section by the contractor for twin tunnels under the River Nile shows that the outside diameter is 6.40 m and lining segment thickness 0.30 m. Also, cross section of single tunnels under the River Nile show that the outside diameter of the tunnel is 9.10 m and lining segment thickness is 0.50 m. Also, tunnels separation distances and dimensions are shown in Fig. 7.

Fig. 5.
Arrangement of TBMs and Positions of Starting Diggings
Source: JICA Project document (2011)

5. Numerical Analysis Procedure

In this study, Finite Element Analysis was conducted using the Finite Element (FE) programs, Ansys, Civil FEM, Plaxis and Rocscience Phase. In Plaxis and Rocscience Phase programs, a 2-D plane strains elements were used for soil modeling and 2-D beam elements for tunnel lining modeling. To simulate the soil behavior, a 3-node triangular element and 15-node triangular element was used in Rocscience Phase program and, Plaxis program, respectively. In Ansys program, element type Plane 42, which is set by the model of plane strains and calculated by Drucker-Prager criteria, was used to simulate of the soil, while tunnel lining was simulated by the element type Plane 82. Regarding the boundary conditions, the model was free at the top side and totally hinged “constrained” at the bottom, right hand and left hand side edges.

5.1. 2D Model Dimensions

All the appropriate dimensions of the base boundary were evaluated; then, the bottom boundary was fixed, and the minimum dimensions of the width of vertical boundaries were considered. The bottom boundary and model width $W$ can be obtained using the following Eqs. (1-2) (Moller, 2006):

$$h = (1.5-2.5)*D$$

(1)

$$W = 2D*(1+H/D)$$

(2)
**Fig. 6.**
Proposed Single and Twin Tunnel System from Station No. 1 to Station No. 5

**Fig. 7.**
Tunnels Separation Distances and Dimensions
It is considered in this study that \( D = 9.10 \) m; thus it yields a minimum dimension of the model \( h = 23 \) m and \( H = 42 \) m. From previous equation \( W \) is taken equal to 100 m as shown in Fig. 8. To find the best dimensional model, it was assumed that the minimum model width \( W = 100 \) m. The model height \( (H) \) was changed incrementally from 30 m to 75 m and it was found that the best model height \( (H) \) should be 55 m (Fig. 9). The 55 m height was the best because it gave the ideal surface settlement and stresses induced at the tunnel liner. Also, if the height is taken more than 55 m, no change occurs in both the settlement and the stresses. Also to determine the best width \( (W) \), it was changed from 60 to 150 m while the height was kept constant at 55 m. It was found that best width \( (W) \) for the model is 120 m (Fig. 10). Surface settlement profile of single tunnels in case of best dimension model \((120*55)\) and surface settlement profile of twin tunnels are shown in Fig. 11 and Fig. 12, respectively.

Fig. 8.
2-D Finite Element Model (Rockscience Phase Program)

5.2. Bending Moment and Displacements

It is so important for the designer to know the internal forces and displacements in order to design the tunnel. The following results show bending moments and settlement of single and twin tunnels. For single tunnel, the vertical displacements and bending moment diagrams are shown in Fig. 13 and Fig. 14, respectively. Moreover, Fig. 15 and Fig. 16 show the bending moment and displacements of the bottom and top tunnels (twin tunnels). Comparing the vertical displacement of the top and bottom fibers in cases of single and twin tunnels it can be noticed that vertical displacement of the top fiber is greater than that of the bottom fiber. This result explains the increase in bending moment at bottom fiber due to the high value of the bottom soil reaction. It is also noticed that, for twin tunnel, the values of stresses at the tunnel lining of the bottom tunnel is nearly double the values for corresponding points at single tunnel. It is clear from the results which are shown in Fig. 17 that in case of construction
of top tunnel before the bottom tunnel, the bending moment will be increased for top tunnel and when constructed bottom tunnel before top tunnel. Bending moment in top tunnel will be decreased. But there is no difference in bending moment of the bottom tunnel before or after construction of top tunnel. Fig. 17 also shows bending moment of bottom tunnel after and before construction of top tunnel.

![Model Height](image1)

**Fig. 9.**
**Optimum Model Height** $H = 55 \text{ m}$

![Model Width](image2)

**Fig. 10.**
**Optimum Model Width** $W = 120 \text{ m}$

![Bed River Nile Settlement Profile for Single Tunnel](image3)

**Fig. 11.**
**Bed River Nile Settlement Profile for Single Tunnel**
Abd-el-rahim H.H.A. et al. Analysis of Different Loads Affecting the Urban Railway Tunnel Systems of Cairo Metro Underneath the River Nile

**Fig. 12.**
Bed River Nile Settlement Profile for Twin Tunnel

**Fig. 13.**
Vertical Displacement of Single Tunnel

**Fig. 14.**
Bending Moment of Single Tunnel

**Fig. 15-1.**
Bending Moment of Top Tunnel

**Fig. 16-1.**
Vertical Displacement for Top Tunnel
5.3. Effect of Train Loads

The effect of train loads on settlements and stresses were evaluated for single and twin tunnels. The loads were 80 kN on the vertical direction and 60 kN on the lateral direction. These loads are concentrated on the tip of the rails as shown in Fig. 18. In the case of single tunnels (double tracks) the obtained results shows that the maximum settlement of the river bed changed from 71.46 to 73.52 mm when train passes through single tunnel, whereas in the case of twin tunnel the settlement changed from 78.85 mm to 80.96 mm when train passes through twin tunnel. These results, shown in Fig. 19, indicate that the train loads slightly increased the surface settlements.

Computed stresses in lining before and after train passing through single and twin tunnels show that stresses slightly decreased when the train passes through both systems as shown in Fig. 20 and Fig. 21, respectively.
Fig. 17-2.
Bending Moment for Top Tunnel Before and After Construction of Bottom Tunnel

Fig. 18-2.
Cross Section for Single Tunnel

Fig. 19-1.
Effect of Train Loads on Surface Settlement for Single Tunnel

Fig. 19-2.
Effect of Train Loads on Surface Settlement for Twin Tunnels

Fig. 20.
Computed Stresses in Lining Before and After Train Passing Through Single Tunnel
5.4. Horizontal Displacements

From previous experiences, it is concluded that construction of tunnels causes movement of surrounding soil horizontally, as shown in Fig. 22. In urban areas, horizontal ground movement causes damage of the buildings near the tunnels. However, when tunnel passes under River Nile, horizontal ground movement causes erosion of bed level of Nile. It is clear from Fig. 22 that the direction of movement of the upper soil is in the direction of the tunnel, but for bottom soil in a direction out of tunnels. The horizontal movement profile of the bed River Nile for the single is shown in Fig. 23 and for twin tunnels is shown in Fig. 24. It is also obtained that a slight difference in horizontal movement at single and twin tunnel systems.

Fig. 21.
Computed Stresses in Lining Before and After Train Passing Through Twin Tunnel

Fig. 22.
Horizontal Movement of Soils Surrounding of the Tunnel
6. Conclusion

Accurate reviewing the results we concluded that:

1. Settlements and bending moments, obtained by Plaxis, Rocscience Phase were very similar. Also, results of stress analysis, obtained by Plaxis and Ansys programs, are mostly convergent. So as to, it is recommended that the Plaxis program is more reliable program for tunnel projects compared to the other used programs (Rocscience Phase and Ansys).

2. All the programs yielded the same dimensions for the optimal model of the tunnel.

3. Increasing of maximum vertical surface displacement of twin tunnel comparing with a single tunnel by 2% (small difference), and also a small difference between horizontal displacements for twin and single tunnel.
4. A higher stress in the lining of the lower tunnel of thickness 0.30 m (case of twin tunnel) is obtained compared with the stress in single tunnel lining of thickness 0.40 m, it was found, stresses in bottom tunnel (twin tunnel system) increased by 100% about stresses in a single tunnel.

5. When trains pass through the tunnel, stresses decrease about 10% for single tunnel and about 5% for twin tunnels.

6. In case of the twin tunnel, construction of the bottom tunnel before the top tunnel is preferable to decrease the stresses in the top tunnel lining.

7. Effect of train loads on the maximum surface settlement and stresses is not significant compared with the dead loads effect.

8. The single tunnel system is the optimum system.

Acknowledgements

Authors would like to acknowledge the providing of data by the members of National Authority of Tunnels in Cairo.

References


Mazek, S.A. 2011. 3-D Nonlinear Numerical Analysis to study the Performance of Twin Tunnel System, Civil Engineering Department, Military Technical College, Cairo, Egypt.


